Study of Simple MPPT Converter Topologies for Grid Integration of Photovoltaic Systems

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Abstract **– This paper presents a study of two simple MPPT converter topologies for grid integration of photovoltaic (PV) systems. A general description and a steady state analysis of the discussed converters are presented. Main operating modes of the converters are explained. Calculations of main circuit element parameters are provided.**

Experimental setups of the MPPT converters with the power of 800 W were developed and verified by means of main operation waveforms. Also, experimental and theoretical boost properties of the studied topologies are compared.

Finally, the integration possibilities of the presented MPPT converters with a grid side inverter are discussed and verified by simulations.

Keywords **– DC-DC power converters, photovoltaic systems, pulse inverters**

I. INTRODUCTION

Distributed generation systems that use renewable energy have great potential to increase the grid potential. Photovoltaic (PV) technology that provides renewable energy is the most popular distributed energy source with zero emissions.

PV cells have nonlinear *U-I* characteristics. The output voltage and power change according to the temperature and irradiation.

Fig. 1. Typical *U-I* and *P-U* characteristics of the PV stack.

Fig. 1 shows typical *U-I* and *P-U* characteristics of a PV stack. It can be seen that maximum power could be obtained only at one certain point – the maximal power point.

To keep the operation at the maximal power point independent of the temperature and irradiation, the maximal power point tracker (MPPT) converter should be used. Fig. 2 illustrates the general block diagram of a MPPT converter for AC or DC load applications in PV systems.

This paper presents a comparative evaluation of a classical boost converter (BC, Fig. 3*a*) and a quasi-Z-source converter (qZSC, Fig. 3*b*).

Fig. 2. General block diagram of a MPPT converter for a PV system.

II.GENERAL DESCRIPTION OF STUDIED TOPOLOGIES

Simple MPPT converter topologies for grid integration of a PV system are shown in Fig. 3. The PWM inverter is replaced with an equivalent resistance R_E . Fig. 3*a* shows a BC which consists of an inductor L_1 , a capacitor C_1 , a diode D , and a switch *S* [1-3]. Fig 3*b* shows a qZSC, which consists of two inductors L_1 , L_2 with equal inductance, two capacitors C_1 , C_2 with equal capacitance, a diode *D*, and a switch *S* across the DC-link [4].

Fig. 3. Simple MPPT converter topologies: BC (a) and qZSC (b).

III. STEADY-STATE ANALYSIS OF TOPOLOGIES OPERATED IN CONTINUOUS CONDUCTION MODE (CCM)

The steady state analysis for all the discussed converters is presented below. This operation comprises two main power conversion states: voltage boost (on-state of the switch *S*) and power transfer (off-state of the switch *S*). The operation period of the switch *S* consists of an on-state t_{ON} and an off-state t_{OFF} :

$$
T = t_{ON} + t_{OFF} \tag{1}
$$

Eq. (1) could also be represented as

$$
\frac{t_{ON}}{T} + \frac{t_{OFF}}{T} = D_{ON} + D_{OFF} = 1,
$$
 (2)

where D_{ON} , D_{OFF} are the duty cycles of the switch *S* on-state and off-state, correspondingly.

A. Boost converter

Fig. 4 shows the equivalent circuits of a classical BC during the on- and off-state of the switch *S*. The switching state diagram of the BC is presented in Fig. 5.

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Fig. 4. Equivalent circuits of a BC: (a) switch *S* is on; (b) switch *S* is off.

From Fig. 4*a*, which represents the conditions when the switch *S* is on with the duration of t_{ON} , we obtain

$$
u_{L1} = U_{I} ; i_{C1} = -\frac{U_{C1}}{R_E}.
$$
 (3)

From Fig. 4*b*, which represents the conditions when the switch *S* is opened with the duration of $(T-t_{ON})$, we obtain

$$
u_{L1} = U_{I} - U_{C1} \,. \tag{4}
$$

At the steady state the average voltage of the inductor over one switching period is zero:

$$
U_{L1} \cdot (t_{ON}) + U_{L1}(t_{OFF}) = 0.
$$
 (5)

Thus, from Eqs. (3) and (5) we obtain

$$
U_{L1} = \overline{U}_{L1} = \frac{U_{IN} \cdot (t_{ON}) + (U_{IN} - U_{C1}) \cdot (1 - t_{ON})}{T} = 0.
$$
 (6)

Accordingly,

$$
U_{C1} = \frac{U_{I N}}{1 - t_{ON}}.
$$
 (7)

The output voltage is

$$
u_{OUT} = U_{C1} = \frac{1}{1 - D_{ON}} \cdot U_{IN} = B \cdot U_{IN} , \qquad (8)
$$

where B is the boost factor of the BC

$$
B = \frac{1}{1 - D_{ON}} \tag{9}
$$

The inductor in the converter will limit the current ripple through the switch *S* during its on-state. Choosing an acceptable peak to peak current ripple $r_{C,\langle\mathcal{C}\rangle}$ the inductance L_1 of the inductor can be calculated as

$$
L_1 = \frac{U_{L1}dt}{di_{L1}}\,. \tag{10}
$$

where

$$
U_{L1} = U_{IN} \; ; \; dt = D_{ON} \cdot T = \frac{D_{ON}}{f} \; ; \; dt_{L1} = \frac{P}{U_{IN}} \cdot r_{C(\%)} \; , \; (11)
$$

Fig. 5. Operation principle of the BC.

Using (10) and (11), the inductance L_I of the inductor can be calculated as

$$
L_1 = \frac{U_{IN}^2 \cdot D_{ON}}{f \cdot P \cdot r_{C,(\%)}},
$$
\n(12)

where P is the power rating of the converter, U_{I} is the input voltage, f is the operation frequency of the converter, and $r_{C_1(\%)}$ is the desired peak to peak current ripple through the inductor $(I_{p-p}/\overline{I}).$

Using the system power rating *P* we can obtain the average current of the inductor *L1*:

$$
\bar{I}_{L1} = \bar{I}_{IN} = \frac{P}{U_{IN}}.
$$
\n(13)

The operating voltages and average currents of the BC during the switch *S* on-state and an off-state are shown in Table I.

The main purpose of the capacitor C_l is to absorb the current ripple and limit the voltage ripple across the load resistance R_E . The voltage ripple across the capacitor can be roughly calculated by

$$
\Delta U_{C1} = \frac{\bar{I}_L \cdot \Delta t}{C_1} \,,\tag{14}
$$

where \bar{I}_{LI} is the average current through the inductor, C_I is the capacitance and *Δt* is the time interval of the on-state of the switch. The capacitance needed to limit the peak to peak output voltage ripple by $r_{V,(%)}$ could be calculated as

$$
C_1 = \frac{P \cdot D_{ON} \cdot (1 - D_{ON})^2}{U_{IN}^2 \cdot f \cdot r_{V(\%)}},
$$
\n(15)

where P is the power rating of the converter, U_{I} is the input voltage, D_{ON} is the duty cycle of the on-state of the switch, f is the operation frequency of the switch *S*, and $r_{V,\ell\%}$ is the

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desired peak to peak voltage ripple across the capacitor (*Up^p/Ū*).

TABLE I OPERATING VOLTAGES AND CURRENTS OF THE BC

B. qZS-Converter

Fig. 6 illustrates the equivalent circuits of the qZSC in both on-state and off-state of the switch *S*. The switching state diagram of the qZSC is presented in Fig. 7.

Fig. 6. Equivalent circuits of the qZSC during the on-state (a) and off-state (b).

Fig. 7. Operation principle of the qZSC.

From Fig. 6*a*, which represents the on-state of the switch *S* with duration *tON*, we obtain

$$
u_{L1} = U_{C2} + U_{I\!N} \, ; \qquad u_{L2} = U_{C1} \, . \tag{16}
$$

$$
u_{DC} = 0; \t u_D = U_{C1} + U_{C2}. \t(17)
$$

From Fig. 6*b*, which represents the off-state of the switch *S* with the duration of $(T-t_{ON})$, we obtain

$$
u_{L1} = U_{I} - U_{C1}; \quad u_{L2} = -U_{C2}. \tag{18}
$$

$$
u_{DC} = U_{C1} - u_{L2} = U_{C1} + U_{C2} \, ; \quad u_D = 0 \, . \tag{19}
$$

At the steady state the average voltage of the inductor over one switching period is zero. Thus, from Eqs. (16) and (18) we obtain

$$
\begin{cases}\nU_{L1} = u_{L1} = \frac{t_{ON} \cdot (U_{C2} + U_N) + (T - t_{ON}) \cdot (U_N - U_{C1})}{T} = 0 \\
U_{L2} = u_{L2} = \frac{t_{ON} \cdot (U_{C1}) + (T - t_{ON}) \cdot (-U_{C2})}{T} = 0\n\end{cases}
$$
\n(20)

Accordingly,

$$
U_{C1} = \frac{1 - D_{ON}}{1 - 2 \cdot D_{ON}} \cdot U_{N} \quad \text{and} \quad U_{C2} = \frac{D_{ON}}{1 - 2 \cdot D_{ON}} \cdot U_{N} \,. \tag{21}
$$

The output voltage is

$$
u_{OUT} = U_{C1} + U_{C2} = \frac{1}{1 - 2D_{ON}} \cdot U_{IN} = B \cdot U_{IN} , \qquad (22)
$$

where B is the boost factor of the qZSC:

$$
B = \frac{1}{1 - 2 \cdot D_{ON}} \tag{23}
$$

Using the system power rating *P* we can obtain the average current of the inductors *L¹* and *L2*:

$$
\bar{I}_{L1} = \bar{I}_{L2} = \bar{I}_{IN} = \frac{P}{U_{IN}},
$$
\n(24)

where $U_{I N}$ and $I_{I N}$ are the input voltage and current of the converter. To obtain the necessary currents of the qZSC we can use Kirchhoff's current law:

$$
\bar{I}_{C1} = \bar{I}_{C2} = \bar{I}_{OUT} - \bar{I}_{L1}.
$$
 (25)

$$
\bar{I}_{D1} = 2\bar{I}_{L1} - \bar{I}_{OUT} \,. \tag{26}
$$

The operating voltages and currents of the qZSC during onand off-states are shown in Table II. The main purpose of capacitors C_1 and C_2 is to absorb the current ripple and limit the voltage ripple across the switch *S*. The capacitor voltage ripple voltage ripple can be roughly calculated by (14).

Time interval	t_{ON}	t_{OFF}
Inductor voltage $(u_{L1} = u_{L2})$	$\cdot \frac{D_{\textit{ON}}}{1-2\cdot D_{\textit{ON}}} \cdot U_{\textit{IN}}$	$-\frac{1-D_{\rm ON}}{1-2\cdot D_{\rm ON}}\cdot U_{\rm IN}$
Output voltage (u _{OUT})	$\frac{1}{1-2\cdot D_{ON}}\cdot U_{IN}$	θ
Output current (I_{OUT})	$P\cdot(1-2\cdot D_{\textit{ON}})$ $\overline{U}_{{I\!\!N}}$	$\frac{2 \cdot P}{U_{N}} \cdot D_{ON}$
Diode D_l voltage (u_D)	$\overline{0}$	$\frac{1}{1-2\cdot D_{on}}\cdot U_{m}$
Capacitor C_l voltage (U_{Cl})	$\frac{1-D_{\scriptscriptstyle ON}}{1-2\cdot D_{\scriptscriptstyle ON}}\cdot U_{\scriptscriptstyle IN}$	
Capacitor C_2 voltage (U_{C_2})	$\frac{D_{\scriptscriptstyle ON}}{1-2\cdot D_{\scriptscriptstyle ON}}\cdot U_{\scriptscriptstyle IN}$	
Input current (IIN)	\boldsymbol{P} U_{N}	
Inductor current $(\bar{I}_{LI} = I_{L2})$	\boldsymbol{P} $\overline{U}_{{\scriptscriptstyle{I\!N}}}$	
Capacitor current $(\bar{I}_{C1} = \bar{I}_{C2})$	I_{DC} - I_{LI}	
Diode current (\bar{I}_D)	$2\cdot \bar{I}_{LI}$ - \bar{I}_{DC}	

TABLE II OPERATING VOLTAGES AND CURRENTS OF THE QZSC

During the off-state, both capacitors of the qZSC are in series (Fig. 6*b*). Assuming that the capacitance should be the same for each capacitor, the capacitance needed to limit the peak to peak DC-link voltage ripple by $r_{V,(\%)}$ could be calculated as

$$
C = \frac{2 \cdot P \cdot D_{ON} \cdot (1 - 2D_{ON})}{U_{IN}^2 \cdot (1 - D_{ON}) \cdot f \cdot r_{V,(\%)}},
$$
 (27)

where *P* is the power rating of the converter, U_{I} is the input voltage, D_{ON} is the duty cycle of on-state, f is the operation frequency of the switch *S*, and $r_{V(\%)}$ is the desired peak to peak voltage ripple across the load R_E (U_{pp}/\bar{U}).

The inductor in the qZSC network will limit the current ripple through the switch *S* during the on-state. Choosing an acceptable peak to peak current ripple $r_{C,\binom{9}{6}}$ the inductance can be calculated by

$$
L = \frac{U_{IN}^2 \cdot (1 - D_{ON}) \cdot D_{ON}}{(1 - 2D_{ON}) \cdot f \cdot P \cdot r_{C(\%)}},
$$
 (28)

where P is the power rating of the converter, U_{I} is the input voltage, U_{CI} is the capacitor's C_I voltage, D_{ON} is the duty cycle of on-states, *f* is the operation frequency of the switch *S*, and $r_{C(%)}$ is the desired peak to peak current ripple through the inductor $(I_{p-p}/\overline{I}).$

IV. EXPERIMENTAL VERIFICATION

To verify the theory discussed above three experimental setups with the rated power of 800 W were developed and tested in the same conditions. It was stated that the input voltage (U_{IN} =40 V) should be boosted two times (U_{OUT} =80 V).

To obtain the desired twofold boost the on-state duty cycles of the switch *S* were set to 0.5 for the BC and 0.25 for the qZSC. As Table III shows, the capacitors and inductors implemented in both topologies have similar values.

TABLE III COMPONENT TYPES AND VALUES USED IN EXPERIMENTS

Component	BC	qZSC
Inductor L_1	$110 \mu H$	
Inductor L_2		$110 \mu H$
Capacitor $C1$	$120 \mu F$	
Capacitor C_2		$120 \mu F$
Diode D	STTH200L06TV1	
Switch S	SKM50GB123D	

Fig. 8 presents the main operating waveforms of the discussed converters. These are input voltage (*UIN*), input current (I_L) , output voltage (U_{OUT}) , and output current (I_{OUT}) . It is obvious that both converters can step up the input voltage two times. Fig. 8 shows that BC features the DC output voltage while the qZSC has the square wave output voltage waveform. The output current and voltage ripple of the BC is almost negligible. However, the qZSC has the input current ripple reduced by 10% as compared to BC, which is especially topical in applications with renewable energy sources. Finally, for the same component types and values the qZSC has smaller ringing in the input voltage profile (which is mostly caused by switching transients), and, consequently, reduced stress of the solar panel and smaller EMI impact.

Fig. 8. Main operation waveforms of the BC (a) and the qZSC (b) MPPTs: input voltage (U_{IN}) and current (I_{IN}), output voltage (U_{OUT}) and current (I_{OUT}).

In the second experiment the voltage boost properties were examined for each converter and compared to those theoretically predicted. Relation between the converter output voltage U_{OUT} and the switch on-state duty cycle D_{ON} is shown in Fig. 9. It was stated that the twofold voltage boost can be achieved with both the BC and the qZSC, though the qZSC requires twice smaller on-state duty cycle *DON* of the switch *S*. It can be explained by the number of energy storage elements that is doubled. Fig. 9 also shows that at a larger D_{ON} value the experimental curve becomes lower than the theoretical curve. This fact can be explained by the voltage drop on the circuit elements, mostly in semiconductors.

Fig. 10 shows the inductance *L* as a function of the boost factor *B* for the discussed converters for the current ripple of

20%. It can be seen that for the same boost factor *B* the inductance of the inductor must be about 40% larger for the BC as compared to the qZSC. In contrast to the BC, the qZSC requires one additional inductor, which could impose an additional space and weight requirements. However, utilizing the coupled inductors with common mode coupling as described in [5], the twice reduced inductance value of each inductor could be assumed for the same input current ripple.

Fig. 11 shows the capacitance *C* as a function of the boost factor *B* for the discussed converters. The capacitance of capacitors C_1 and C_2 of the qZSC for the twofold boost and assumed 5% ripple should be two times higher than for BC and in the case of twofold boost, the difference is even.

Fig. 9. Experimental and theoretical boost properties of the BC (a) and the $qZSC$ (b).

Fig. 10. Inductance of inductors of the BC and the qZSC as a function of the boost factor.

Fig. 11. Capacitance of capacitors of the BC and the qZSC as a function of the boost factor.

V. INTEGRATION POSSIBILITIES WITH A GRID SIDE INVERTER

In most cases the connection of PV with a grid is realized by the topology presented in Fig. 2. Since the DC voltage generated by a PV stack varies widely, a MPPT converter is essential to generate a regulated voltage. A DC-AC inverter is essential to provide useful AC power at 50 Hz frequency. An

output LC filter connected to the inverter filters the switching frequency harmonics and generates a high quality sinusoidal AC waveform suitable for the dedicated loads.

This section discusses the possibilities of integration of discussed MPPT converters with the grid side inverter in order to reduce the number of switching elements, simplify the control circuits and increase the power density.

A. Boost converter

The BC cannot be integrated to the grid side inverter and could be only implemented as an auxiliary converter with separate control (Fig. 12). The presented cascaded arrangement of the BC and the grid side inverter increases both the complexity of the power circuit and the controller and the cost and space requirements. Moreover, the increased number of power switches results in a lower efficiency.

The full-bridge inverter with an LC filter inverts the intermediate DC link voltage into AC voltage. The unipolar modulation technique is used for the inverter control to reduce the switching losses and output filter size [6]. The sine wave signal and the inverter sine wave signal are compared there with a bipolar triangle signal in order to obtain gate signals for transistors T_1 and T_3 . The inversed signals drive the opposite transistors *T²* and *T4*.

Fig. 12. BC based interface converter for grid integration of PV systems.

If the small voltage drop and phase shift in the LC filter are neglected, then the output voltage of the inverter is

$$
u_{grid} = U_{IN} \cdot \frac{M_i}{1 - D_{ON}} \cdot \sin(\omega t), \qquad (29)
$$

where M_i is the modulation index of the inverter. Fig. 13 shows the simulation results of the topology presented in Fig. 12. It was assumed that the output voltage of the PV stack is 160 VDC. The boost converter operating with the duty cycle of 0.5 is stepping up the input voltage to the level of 320 VDC, which is essential to generate the grid side AC voltage with an rms value of 230 V.

Fig. 13. Simulation results of the BC based interface converter.

B. qZS-Converter

A marked advantage of the qZSC is that it could be fully integrated with the grid side inverter (Fig. 14). The topology presented is also referred to as a quasi-Z-source inverter (qZSI, [7, 8]), consisting of the unique LC and diode network (qZS-network) connected to the inverter bridge. The function of the switch *S* (Fig. 3*b*) could be fully replaced by the special switching state of the inverter – the shoot-through state, when both switches of one inverter leg are simultaneously switched on. The qZS-network will effectively protect the circuit from damage when the shoot-through occurs and also could boost the input voltage to a higher level simply by the variation of the shoot-through duty cycle. Neglecting losses in components the output voltage of the inverter could be estimated as

$$
u_{grid} = U_{IN} \cdot B \cdot M_i \cdot \sin(\omega t) = U_{IN} \cdot \frac{1 - D_S}{1 - 2D_S} \cdot \sin(\omega t), \quad (30)
$$

where D_S is the shoot-through duty cycle.

Fig. 14. qZSC based interface converter for grid integration of PV systems.

Fig. 15 shows the simulation results of the qZSC based interface converter for grid integration of PV systems. It was assumed that the output voltage of the PV stack is 160 VDC. In order to obtain the grid side AC voltage with an rms value of 230 V the shoot-through duty cycle was set to 0.33. The intermediate DC-link voltage U_{DC} was stepped up to the level of 490 V, which is essential to generate the sinusoidal voltage at the given modulation factor $(M_i=1-D_s=0.66)$ and with the required amplitude of 320 V.

Fig. 15. Simulation results of the qZSC based interface converter.

VI. CONCLUSIONS

This paper presents a comparative study of simple MPPT converter topologies for the PV system integration with a grid. The MPPT converter topologies were described in detail and an analysis of operation states and calculations of voltages, currents and circuit parameters were presented. The experimental results showed that the discussed converters have necessary voltage boost properties and can be used for the MPPT function.

Finally, the integration possibilities of the presented MPPT converters with a grid side inverter were discussed and verified by simulations. The simulation results show that the discussed converters which are coupled with a grid side inverter can boost input DC voltage and can ensure sinusoidal voltage with an rms value of 230V at the AC load or grid.

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